1. Prove that for all positive integers n,

$$1^3 + 2^3 + \dots + n^3 = \left\lceil \frac{n(n+1)}{2} \right\rceil^2$$
.

2. Prove that for all positive integers $n \geq 2$,

$$1 \cdot 2 + 2 \cdot 3 + 3 \cdot 4 + \dots + (n-1)n = \frac{(n-1)n(n+1)}{3}.$$