Name: _

- 1. Suppose $G = \{e, a, b, c\}$ is the group defined by the following Cayley table.

Let $H = \langle a \rangle$.

- (a) Find the left cosets of H in G.
- (b) Find the right cosets of H in G.
- (c) Determine |G:H|
- 2. Let A, B and C be groups. Suppose A is a proper sugroup of B and B is a proper subgroup of C. If |A| = 30 and |C| = 900, what are possible orders of B? Explain your answer!
- 3. Let G be a group with |G| = 95. Let $x, y \in G$, where both x and y are nonidentity elements and $|x| \neq |y|$. Prove that the only subgroup of G that contains both x and y is G.